Characterizing arid region alluvial fan surface roughness with airborne laser swath mapping digital topographic data

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[1] Range-front alluvial fan deposition in arid environments is episodic and results in multiple fan surfaces and ages. These distinct landforms are often defined by descriptions of their surface morphology, desert varnish accumulation, clast rubification, desert pavement formation, soil development, and stratigraphy. Although quantifying surface roughness differences between alluvial fan units has proven to be difficult in the past, high-resolution airborne laser swath mapping (ALSM) digital topographic data are now providing researchers with an opportunity to study topography in unprecedented detail. Here we use ALSM data to calculate surface roughness on two alluvial fans in northern Death Valley, California. We define surface roughness as the standard deviation of slope in a 5-m by 5-m moving window. Comparison of surface roughness values between mapped fan surfaces shows that each unit is statistically unique at the 99% confidence level. Furthermore, there is an obvious smoothing trend from the presently active channel to a deposit with cosmogenic \(^{10}\)Be and \(^{26}\)Cl surface exposure ages of \(~\)70 ka. Beyond 70 ka, alluvial landforms become progressively rougher with age. These data suggest that alluvial fans in arid regions smooth out with time until a threshold is crossed where roughness increases at greater wavelength with age as a result of surface runof and headward tributary incision into the oldest surfaces.


1. Introduction

[2] Alluvial fans are common features along the piedmonts of steep mountain fronts where streams exit the narrow confines of their source canyons, resulting in a reduction in stream power and a consequent decrease in the ability of the streams to carry large sediment loads [Bull, 1977]. In arid environments, this range-front deposition tends to be episodic, can be punctuated by erosion, and is commonly expressed as multiple generations of alluvial fan surfaces [Bull, 1991]. Alluvial fans are important recorders of both climatic and tectonic signals; alluvium of varying age can contain vast amounts of information about climatic influences on deposition, or lack thereof, as well as rates and styles of tectonism and as such, have been studied extensively [Gilbert, 1877; Davis, 1905; Blackwelder, 1931; Denny, 1967; Bull, 1977; Wallace, 1977; Bull, 1984; Wells et al., 1987; Lubetkin and Clark, 1988; Bull, 1991; Whipple and Dunne, 1992; Ritter et al., 1993; Bierman et al., 1995; Matmon et al., 2005; Nichols et al., 2006; Bull, 2007].

[3] Discrete alluvial units are often defined by descriptions of surface morphology, desert varnish accumulation, clast rubification, desert pavement formation, soil development, and stratigraphic relationships [Wells et al., 1987; Bull, 1991; Ritter et al., 1993]. In particular, studies of soil development on desert piedmonts have been especially useful in deciphering ages of alluvial landforms and rates of fan deposition [Birkeland, 1999]. Recent advances in Quaternary geochronology are allowing researchers to further quantify rates of arid-region geomorphic processes [e.g., Nichols et al., 2002, 2005, 2006; Matmon et al., 2006].

[4] In general, alluvial fan units are mapped on aerial photographs and topographic maps using the above criteria, in conjunction with elevation above active channels, in order to determine lithostratigraphic divisions. Quantifying the topographic characteristics and differences between multiple fan surfaces, however, has been difficult with previously available maps and remotely sensed data because they generally lack the spatial resolution necessary to make a quantitative comparison between individual alluvial fan deposits [e.g., Farr and Chadwick, 1996]. Field techniques, such as clast-size counts or topographic surveying, while useful, are labor-intensive and usually limited in their spatial extent, therefore providing data on only a small segment of any single alluvial unit. Recently, however, the emergence of high-resolution airborne laser swath mapping (ALSM; also known as light detection and ranging or LiDAR) technology has renewed interest in the quantitative characterization of alluvial and colluvial landforms [McKean and Roering, 2004; Glenn et al., 2006; Staley et al., 2006].

[5] ALSM digital topographic data are now providing researchers with the opportunity to study landforms in
The high resolution of ALSM digital topographic data, generally on the order of 0.5 to 3 m in the horizontal and 10 to 20 cm vertically, allows the construction of very accurate digital elevation models, from which a number of surface characteristics can be readily extracted. Of particular interest to differentiating and quantifying alluvial landform development is surface roughness, which is often one of the most obvious features distinguishing fans of different age, yet has traditionally been one of the hardest metrics to quantify.

Previous studies using ALSM digital elevation data to differentiate, characterize, and map landslide morphology have shown that surface roughness may be evaluated in a variety of ways. McKean and Roering (2004) analyzed ALSM data to objectively map the spatial and temporal characteristics of a landslide in New Zealand on the basis of topographic roughness determined by eigenvector ratios. In a similar study, based on various measures of topographic roughness, Glenn et al. (2006) used surface roughness, slope, semivariance, and fractal dimension to characterize and differentiate landslide morphology and activity. In addition, Staley et al. (2006) used ALSM data to investigate depositional patterns on small debris flow fans in central Death Valley through the analysis of profile curvature and fan gradient.

Here we use the classic methods of topographic variability, degree of varnish accumulation, soil development, and clast size counts, combined with a quantitative measure of surface roughness calculated as the standard deviation of slope from ALSM data, to characterize and differentiate alluvial fan surfaces with different relative ages. Our calculation of surface roughness differs from previous studies in that it allows us to investigate topographic patterns at scales of individual bars and swales to entire alluvial fan systems. Specifically, this study is focused on two alluvial fan complexes in northern Death Valley, along the western Grapevine Mountains piedmont (Figures 1 and 2). We show that fan units of different relative age can be successfully delimited through statistical

**Figure 1.** Location map of the study sites and surrounding areas. Circed numbers represent the locations of the two alluvial fans in northern Death Valley used in this study. Location 1 refers to the fan in Figures 2a and 3. Location 2 refers to the fan in Figures 2b and 4. DSV, Deep Springs Valley; EV, Eureka Valley; LCR, Last Chance Range; GM, Grapevine Mountains; CM, Cottonwood Mountains; SV, Saline Valley; FM, Funeral Mountains; BM, Black Mountains; YM, Yucca Mountain.
cally unique surface roughness values extracted from high-resolution ALSM data and propose a model for the evolution of alluvial surfaces through time on the basis of the surface roughness calculations. Furthermore, our results suggest that ALSM data can be used to efficiently and objectively map alluvial landforms.

2. Geologic Setting

Death Valley is located along the western edge of the Great Basin, at the transition between the extensional Basin and Range Province and the strike-slip faults comprising the eastern California shear zone. Death Valley is a pull-apart basin formed by a step-over between the right-lateral southern Death Valley and northern Death Valley fault zones. Displacement along a down-to-the-west normal fault forms the deep, central basin between the two strike-slip fault systems [Burchfiel and Stewart, 1966]. Opening of the basin as a result of continued tectonic activity since at least the Miocene has produced the accommodation space necessary for continuous deposition of alluvial deposits [Hamilton, 1988; Wernicke et al., 1988; Burchfiel et al., 1995]. Rates of tectonic activity range from 1 to 3 mm/yr along the normal fault in central Death Valley to ~4.5 mm/yr on the northern Death Valley fault zone [Brogan et al., 1991; Klinger, 2001; Knott et al., 2002; Frankel et al., 2007].

Climate in the region during late Pleistocene and Holocene time has been dominated by two wet, cold periods and two warm, dry intervals [Li et al., 1996; Lowenstein et al., 1999]. Perennial lakes existed in the central basin during the penultimate glacial advance from ~128 to 186 ka (oxygen isotope stage 6) and the last glacial maximum from ~12 to 35 ka (oxygen isotope stage 2) when the climate was cooler and wetter [Lowenstein et al., 1999]. From 60 to 120 ka, climate is thought to have been similar to the aridity characterizing the Holocene environment [Lowenstein et al., 1999]. The period from 35 to 60 ka was a time of unstable climate and hence, fluctuating lake levels. The present-day arid climate results from the large rain shadow produced by the Sierra Nevada, Inyo Mountains, and Panamint Mountains (Figure 1) [Poage and Chamberlain, 2002]. With elevations up to ~4400 m, these three ranges inhibit the eastward migration of moist air masses coming from the Pacific Ocean. As a result, modern-day precipitation in central Death Valley is a sparse ~6 cm/yr (Western Region Climate Center, http://www.wrccl.dri.edu).

3. Alluvial Fan Stratigraphy and Surface Characteristics

Alluvial fans are pervasive piedmont features at the base of the major mountain ranges bounding Death Valley.
to the east and west (Figures 1 and 2). Relatively small, steep alluvial fans deposited mainly in debris flow events are found at the base of the Black Mountains, where they are commonly offset by the range-bounding normal fault [Denny, 1965; Brogan et al., 1991; Burchfiel et al., 1995; Staley et al., 2006]. Throughout much of the rest of the Death Valley basin, such as along the eastern Panamint and western Funeral and Grapevine Mountains piedmonts (Figures 1 and 2), alluvial fans are spatially more extensive, forming continuous bajada-like surfaces. Alluvial fans in these locations are generally thought to be deposited through a combination of sheet-wash and debris flow events [Denny, 1965; Hunt and Mabey, 1966; Bull, 1977; Blair, 2000].

![Figure 3](insert)

Figure 3. Geologic and surface roughness maps of the alluvial fan at location 1 in Figure 1. (a) Surficial geologic map of the alluvial fan. Arrows delineate the trace of the dextral-slip northern Death Valley fault zone [Frankel et al., 2007]. Faults are left off map for clarity. See text and Table 1 for detailed descriptions of map units. Modified from Klinger [2001]. (b) Surface roughness map of the alluvial fan in Figure 3a. Roughness values were calculated as the standard deviation of slope over a 5 m^2 area. Note the similarity with the geologic map in Figure 3a. Scale bar represents values of the standard deviation of slope, which is the metric used in this study to measure surface roughness.

[11] Previous work, both in Death Valley and throughout southwestern North America, has defined a consistent alluvial fan stratigraphy for the region [Denny, 1965; Hunt and Mabey, 1966; Moring, 1986; Bull, 1991; Klinger, 2001]. The alluvial fans in our two study areas comprise eight distinct lithostratigraphic units: Q4b, Q4a, Q3c, Q3b, Q3a, Q2c, Q2b, and Q2a (Figures 3 and 4). Unit Q4b represents active alluvial channels and occupies the lowest topographic position in the landscape. Unit Q2a is the oldest alluvial landform in the study area and thus stands topographically higher than the other units (Figures 3 and 4). Each of these units is described briefly below. More detailed descriptions of the alluvial fan stratigraphy can be found in the works of Bull [1991] and Klinger [2001, 2002]. In addition, we measured clast sizes at 1-m increments for 50 m on each surface in the midsection of the fans to further characterize the units on the basis of field observations. Table 1 provides a synopsis of the characteristics of each of the mapped surfaces in the study area.

3.1. Q4b

[12] This is the youngest surface mapped in the study area (Figure 3a) and is defined as the active alluvial fan channels. The alluvium in this deposit is generally distributed bimodally, with bars of coarse cobbles and boulders, and swales (channels) consisting of finer-grained pebbles and sand (Figures 5a and 6). No desert varnish, soil, or desert pavement are developed on this surface. Relief on this surface ranges from 0.5 to 1.5 m.

3.2. Q4a

[13] The Q4a surface (Figure 3a) is characterized by prominent bar and swale topography similar to that of unit Q4b, with clasts ranging from pebble to boulder in size (Figures 5b and 6). Little to no varnish or rubification is developed on clasts. Locally, immature patches of pavement are observed in small, to 6 m^2 areas. The Q4a surface commonly has a thin (up to 5 cm thick), Av soil horizon. This unit is the most recently abandoned surface found on the alluvial fans and is generally 0.5 to 1 m above the active channels.

3.3. Q3c

[14] A distinct bar-and-swale topography is still present on the Q3c surface with 0.5 to 1.0 m of relief (Figure 3a), however, an immature pavement, composed mainly of finer-grained clasts has started to form (Figure 5c). In addition, clasts, which range in size from pebbles to boulders (Figure 6), have a light coating of varnish and are slightly rubified. Soils are characterized by a 10-cm-thick Av horizon, a 30-cm-thick B horizon with small amounts of minor salt (Stage I), carbonate, and clay-film accumulations.

3.4. Q3b

[15] The Q3b surface (Figure 3a) is characterized by an intermediate desert pavement and a bar-and-swale morphology with moderate relief of 0.25 to 0.75 m (Figure 5d). Clasts, which range in size from pebbles to large cobbles/small boulders (Figure 6), are moderately varnished and rubified. Soils are characterized by a ≥10-cm-thick Av horizon, a ~30-cm-thick B horizon with small amounts of...
salt and carbonate accumulations (Stage 1+) and moderate clay film development. In addition, weak soil development, ~10 cm thick, has altered the C horizon.

3.5. Q3a

[16] The bar-and-swale topography on the Q3a surface (Figure 3a) is subdued (0.1 to 0.5 m of relief), yet still observable, with clasts ranging from pebbles to cobbles in size (Figures 5e and 6). The surface is characterized by a well-packed pavement and clasts that are moderately to heavily varnished and rubified. A moderately well-developed soil is found beneath the surface and is distinguished by a 10- to 20-cm-thick Av horizon, a 40- to 50-cm-thick B horizon with Stage II salt and carbonate accumulations, and a weakly developed C horizon.

3.6. Q2c

[17] Clasts on the Q2c surface (Figure 3a) range from cobbles to small boulders in size (Figure 6). The clasts are tightly packed and form a mature desert pavement. The

Table 1. Northern Death Valley Alluvial Fan Characteristics

<table>
<thead>
<tr>
<th>Unit</th>
<th>Desert Pavement Development</th>
<th>Bar and Swale Structure</th>
<th>Clast Size Distribution, cm</th>
<th>Surface Roughness, $\sigma_m$</th>
<th>Number of Roughness Measurements Extracted</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Bar and Swale Structure</td>
<td>Clast Size Distribution, cm</td>
<td>Surface Roughness, $\sigma_m$</td>
<td>Number of Roughness Measurements Extracted</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Morphology</td>
<td>Relief, m</td>
<td>Min.</td>
<td>Max.</td>
</tr>
<tr>
<td>Q4b</td>
<td>none</td>
<td>prominent</td>
<td>0.5 to 1.5</td>
<td>2</td>
<td>85</td>
</tr>
<tr>
<td>Q4a</td>
<td>none/immature</td>
<td>prominent</td>
<td>0.5 to 1.25</td>
<td>2</td>
<td>65</td>
</tr>
<tr>
<td>Q3c</td>
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<td>well-defined</td>
<td>0.5 to 1.0</td>
<td>1</td>
<td>78</td>
</tr>
<tr>
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<td>subdued</td>
<td>0.25 to 0.75</td>
<td>2</td>
<td>52</td>
</tr>
<tr>
<td>Q3a</td>
<td>mature</td>
<td>subdued</td>
<td>0.1 to 0.5</td>
<td>2</td>
<td>12</td>
</tr>
<tr>
<td>Q2c</td>
<td>mature/mature</td>
<td>none/subdued</td>
<td>0 to 0.25</td>
<td>4</td>
<td>55</td>
</tr>
<tr>
<td>Q2b</td>
<td>moderate/mature</td>
<td>none/subdued</td>
<td>0 to 0.25</td>
<td>4</td>
<td>55</td>
</tr>
</tbody>
</table>

*Clast size distributions were determined from a count of 50 clasts at one clast/meter for a 50-m segment of each surface in the midsection of the alluvial fan.
morphology of the Q2c unit is characterized by highly subdued to nonexistent bar-and-swale morphology (Figure 5f). Tops of clasts are heavily varnished and clast undersides are highly rubified. Beneath the Q2c surface a 50+/-cm-thick soil is developed. The soil is characterized by a 10- to 20-cm-thick A\textsubscript{v} horizon with clay film accumulation in its lower half; a middle B\textsubscript{t} horizon with carbonate and salt development; and lower B\textsubscript{k} horizon with moderate carbonate accumulation (Stage III). The Q2c surface in our study area is ~70 ka, based on \textsuperscript{10}Be and \textsuperscript{36}Cl cosmogenic nuclide surface exposure geochronology [Frankel et al., 2007].

3.7. Q2b

The Q2b unit (Figure 4a) is characterized by smooth pavements that are moderately dissected, forming rounded hillslopes. The surface of the Q2b unit generally has a subdued bar-and-swale morphology with 0 to 0.25 m of local relief (Figure 5g). Clasts range in size from pebbles to

**Figure 5.** Photographs showing examples of the eight alluvial fan units mapped in northern Death Valley. (a) Unit Q4b. (b) Unit Q4a. (c) Unit Q3c. (d) Unit Q3b. (e) Unit Q3a. (f) Unit Q2c. (g) Unit Q2b. (h) Unit Q2a. Note the progression from the prominent bar and swale topography of the youngest units in Figures 5a, 5b, and 5c to the planar intermediate-age surface in Figure 5f and the more rounded surfaces in Figures 5g and 5h. See Table 1 and text for more detailed descriptions of each unit.
Figure 6. Box and whisker plot of clast sizes from each alluvial fan unit in the study area. Clast counts were conducted by measuring the clast size at 1-m increments for 50 m on each surface in the midsection of the fan. A total of 50 clasts were measured on each surface. Horizontal bar in the center of the box represents the mean clast size. The limits of each box are the 25th and 75th percentiles. Whiskers (bars extending from the boxes) define the 10th and 90th percentiles and the black dots represent the 5th and 95th percentiles for clast sizes in each unit.

small boulders and are packed together in a moderately- to well-developed pavement (Figure 6). Varnish development is generally moderate to high and clasts are highly rubified. A mature soil is developed beneath the Q2b surface and is characterized by a 10- to 20-cm-thick Av horizon, a 20- to 60-cm-thick Bt horizon, and a 50- to 100-cm-thick Bk horizon with Stage III carbonate development.

3.8. Q2a

This unit is the oldest surface analyzed in our study (Figure 4a). The Q2a surface is generally composed of the incised remains of pavements forming convex hillslopes (Figure 5h). Clasts range in size from pebbles to boulders and are generally moderately varnished and moderately to heavily rubified (Figure 6). Soil formed beneath the surface is characterized by a 10- to 20-cm-thick Av horizon, a Bt horizon up to 100 cm thick, and a 100- to 200-cm-thick Bk horizon with Stage IV carbonate development. Where bar and swale topography is present on this surface it is generally subdued, having relief on the order of 0 to 0.25 m.

Each of these units is identifiable and mappable from both field observations and high-resolution ALSM digital topographic data. In addition, individual units possess a distinct topographic signature, which can be readily extracted from ALSM data to quantify the dominant geomorphic characteristics of these deposits.

4. Airborne Laser Swath Mapping

Airborne laser swath mapping (ALSM) digital topographic data have several advantages over more common forms of “static” remote sensing technology such as aerial photographs or satellite imagery. ALSM data can be manipulated in a geographic information system to extract features from the landscape such as elevation, slope, aspect, and curvature, among others. Moreover, detailed surveying of landforms, which takes days to weeks with traditional methods, can be accomplished in a matter of hours with ALSM data.

The ALSM data used in this study were acquired by the National Center for Airborne Laser Mapping at the University of Florida [Carter et al., 2001] using a Cessna 337 twin-engine aircraft equipped with a Optech Model ALTM 1233 laser mapping system. The 33 Hz laser source was flown over the southern part of the study area (location 1 in Figure 1) at an elevation of 600 m above ground level and at an elevation of 820 m above ground level over the northern study site (location 2 in Figure 1) at an average speed of 60 m/s. The difference in elevation between the two study sites is a function of the amount of topographic relief along the range-front in each region and does not affect the final resolution of the data. First and last returns, as well as the intensity of each laser pulse, were recorded. The sparse vegetation in the study area is ideal for ALSM data acquisition because the removal of data points related to laser returns from the tops of flora does not reduce the point density of bare-earth shots, as it might in a heavily canopied region. Individual bare-earth data points were aligned in an equally spaced grid at 1-m intervals and fit with a smooth surface through a kriging algorithm using Surfer software. This produced a digital elevation model from the rasterized grid with 1-m horizontal resolution and 5- to 10-cm vertical accuracy [e.g., Krabill et al., 1995; Burroughs and McDonnell, 1998; Shrestha et al., 1999; Carter et al., 2001, 2003; Sartori, 2005; Chaplot et al., 2006]. The grid was then imported into ArcInfo, which was used for all topographic analyses.

5. Surface Roughness

Surface morphology is one of the most widely used criteria to distinguish alluvial fans of different ages [e.g., Wells et al., 1987; Bull, 1991; Ritter et al., 1993]. Previous studies suggest that the relative age of alluvial deposits is manifested by topographic variability, with fan surfaces tending to become smoother with increasing age [Bull, 1977, 1991; Matmon et al., 2006]. We exploit the high resolution of ALSM-derived digital elevation models to quantify changes in alluvial fan surface roughness through time. Although there are many ways in which to measure the texture of alluvial and colluvial material [e.g., McKean and Roering, 2004; Glenn et al., 2006], we define surface roughness as the standard deviation of slope. We choose to calculate the roughness metric in this way because it allows us to average out surface features over a 5 m by 5 m area, thereby eliminating any anomalies related to individual boulders or the occasional large creosote bush. Furthermore, taking this approach to calculating surface roughness accounts more readily for the wavelengths (~5 to 10 m) of bar and swale morphology that are commonly observed in arid alluvial environments.

5.1. Standard Deviation of Slope

The standard deviation of slope was calculated by first deriving a slope map from the 1-m-resolution, ALSM-derived digital elevation model. Slope, $m$, is defined for the
values were the standard deviation of slope or surface roughness: 

\[ \sigma_m = \sqrt{\frac{\sum_{i=1}^{n} (m_i - \bar{m})^2}{n}}, \]  

(4)

where \( \sigma_m \) is the standard deviation of slope or surface roughness, \( n \) is the number of samples in the population, which in our analysis ranges from nine samples for a three cell by three cell area to 40,000 samples for a 200 cell by 200 cell region. \( m_i \) is the value of one specific sample within the sampling area, and \( \bar{m} \) is the population mean [Taylor, 1997]. Because slope values are determined across a 3 m by 3 m window and \( \sigma_m \) values are computed from a subsequent filter of the slope map, surface roughness is averaged over areas ranging from a 5 m² area for a three cell by three cell moving window to a 202 m² area for a 200 cell by 200 cell window.

5.2. Surface Roughness Results

[26] Approximately 73,000 individual \( \sigma_m \) values were extracted from the eight mapped fan units in the study area for each standard deviation window size (Table 1). Points were collected from the center of representative portions of each surface to avoid anomalously high surface roughness values associated with parts of the landscape such as the steep channel walls incised through the fans (Figures 3 and 4). These data illustrate the distinct character of each surface and reveal a trend of decreasing roughness with increasing age when roughness is analyzed over a 5 m² area (Figure 8). On the oldest surfaces, this pattern is reversed, with surface roughness and age becoming positively correlated on the

![Figure 8](image-url)
values across the study area clearly illustrate the utility of
and $s = f_{\text{Borradaile}}(\text{Plots showing mean surface roughness versus window size for the Q4b, Q4a, Q3c, Q3b, Q3a, and Q2c surfaces. Window size ranges from 5 m by 5 m to 102 m by 102 m.})$ (Figure 9a). Older surfaces have topographic signatures that are defined by the longer wavelengths of convex hillslopes incised by tributary channels. See text for further discussion.

oldest fan deposits in the study area (Figure 8). In addition, younger surfaces exhibit a higher variance in surface roughness values, which progressively decreases with increasing age (Figure 8).

[27] When compared with previously mapped alluvial fan units in northern Death Valley (Figures 3a and 3b), maps of $\sigma_m$ values across the study area clearly illustrate the utility of this metric in characterizing and defining individual lithostratigraphic units (Figures 3b and 4b). Most prominent among these is the Q2c surface, which is the smoothest and most stable alluvial landform in the region (Figure 3b). Other alluvial units, although not as well defined, are still clearly distinguishable when compared with geologic observations (Figures 3 and 4).

[28] Calculation of surface roughness at multiple length scales (i.e., by determining $\sigma_m$ in moving windows of different size) also brings out a number of interesting patterns in the landscape (Figure 9). When mean surface roughness is plotted against the size of the moving window over which those values are determined, each surface is characterized by an initial increase in surface roughness with increased window size (Figure 9). Eventually each unit reaches a point where roughness no longer increases as a function of window size (e.g., “interface width” of Barabasi and Stanley [1995]) and roughness values eventually converge at the longest length scales (Figure 9a). In general, individual surfaces have distinct saturation lengths, with an increase in length scale corresponding to an increase in surface age (Figure 9).

5.3. Statistical Analysis

[29] Although the values of surface roughness on each of the eight alluvial fan units appear to be derived from unique populations (Figure 8), we quantitatively test this supposition using a Kolmogorov-Smirnov test. The Kolmogorov-Smirnov test was chosen because it does not make any assumptions regarding the distribution of sample populations, allows populations of different size to be directly compared to one another, and is most effective when applied to large ($n \geq 40$) data sets [Borradaile, 2003]. The test relies on the maximum difference between the cumulative frequency distributions of two sample populations (Figure 10 and auxiliary material Figure S1):

$$D = \max(|F_1(x) - F_2(x)|), \quad (5)$$

where $D$ is the Kolmogorov-Smirnov test statistic (D statistic), and $F_1(x)$ and $F_2(x)$ are the cumulative frequency distributions of two sample populations [Davis, 2002]. $D$ is compared against a critical value, $D_\alpha$, for a given level of significance defined as

$$D_\alpha = f_\alpha \sqrt{N}, \quad (6)$$

where

$$N = \sqrt{\frac{n_1 + n_2}{n_1 n_2}}, \quad (7)$$

and $f_\alpha$ is a coefficient specific to the confidence level for the critical value of $D_\alpha$. The $f_\alpha$ coefficient is equal to 1.36 for the 95% confidence level and 1.63 for the 99% confidence level. $n_1$ and $n_2$ are simply the number of samples in the cumulative distribution functions, $F_1(x)$ and $F_2(x)$ [Chakravarti et al., 1967; Borradaile, 2003].

5.4. Kolmogorov-Smirnov Test Results

[30] Kolmogorov-Smirnov analyses ultimately test for the existence of a null hypothesis. Here the null hypothesis is that surface-roughness values for each mapped alluvial fan unit (Figures 3 and 4) are derived from the same sample population. Each mapped alluvial fan surface was compared to the two surfaces adjacent to it in terms of relative age

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1Auxiliary materials are available in the HTML. doi:10.1029/2006JF000644.
Table 2. Kolmogorov-Smirnov Test Results

<table>
<thead>
<tr>
<th>Alluvial Fan Unit Comparison</th>
<th>Significance Level, $\alpha$</th>
<th>P Value $^b$</th>
<th>D Statistic $^c$</th>
<th>$N$</th>
<th>$n_1+n_2/n_1n_2$ $^d$</th>
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</thead>
<tbody>
<tr>
<td>Q2a versus Q2b</td>
<td>0.01</td>
<td>$1.5 \times 10^{-49}$</td>
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<td>0.0000274</td>
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<td>Q3a versus Q3b</td>
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<tr>
<td>Q4a versus Q4b</td>
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<tr>
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<td>0.3083</td>
<td>0.000302</td>
<td></td>
</tr>
<tr>
<td>Q2b versus Q2c</td>
<td>0.01</td>
<td>$8.0 \times 10^{-14}$</td>
<td>0.0683</td>
<td>0.000216</td>
<td></td>
</tr>
</tbody>
</table>

$^a$This represents a confidence level of 99% ($1 - \alpha$).

$^b$The P value is the probability that the null hypothesis (i.e., the likelihood that the two samples came from the same population) is true. If the P value is less than $\alpha$, then the null hypothesis can be rejected.

$^c$The D statistic is the maximum difference between the cumulative frequency plots of two populations.

$^d$This is the normalization coefficient for two population sizes, $n_1$ and $n_2$.
manner (Figure 11). Surface roughness values, when plotted against relative fan-unit age (Figure 8), bring to light an interesting pattern, which previously has only been described through qualitative field observations [e.g., Bull, 1991]. The youngest alluvial fan surfaces, Q4b, Q4a, and Q3c, have the highest surface roughness values (Table 1 and Figure 8). In addition, the youngest surfaces have the largest variance in the surface roughness metric (Table 1 and Figure 8). This pattern results from freshly deposited clasts of different sizes being sequestered into bars and swales. In general, channel bars are composed of larger clasts and swales are filled with finer-grained material (Figure 5).

[33] Inasmuch as relatively coarse-grained alluvium defines bars, and swales comprise finer grains, surface roughness does not vary strictly as a function of clast size. The resolution of the digital elevation model, from which slope values were derived, is 1 m. This window is larger than even the maximum clast size found on any individual fan surface in the study area (Table 1 and Figure 6). Therefore our calculations of surface roughness take into account only the medium wavelength (~5 to 10 m) bar-and-swale structures that dominate the surface morphology of alluvial fans. We note, however, that clast size may influence the formation and preservation of the bar-and-swale structures, as fans tend to be rougher (higher standard deviation of slope) where mean clast sizes are larger, which leads to a higher angle of repose, and where field observations suggest more prominent expression of bar-and-swale morphology (Figures 5, 6, and 8).

[34] As fan surfaces increase in age, surface roughness decreases from the youngest unit, Q4b, to the most stable, smoothest fan surface, Q2c (Figure 8). Previous work defined the age of the Q2c surface to be ~70 ka, on the basis of in situ 10Be and 36Cl cosmogenic nuclide geochronology [Frankel et al., 2007]. Although fan surfaces younger than the Q2c surface have no absolute age control at present, soil formation and varnish accumulation on the Q4 and Q3 deposits suggest that fan smoothing occurs rapidly in the first few thousand years after deposition. From this point until ~70,000 years after deposition, smoothing of the fan surface proceeds ever more slowly with time. On surfaces older than ~70 ka, the steep walls of channels that have incised through the most stable alluvial surface, Q2c, begin to erode by headward tributary incision, and consume the once-planar surface. As this erosion proceeds, the older surfaces, Q2a and Q2b, become increasingly rougher with increasing age as the alluvial fans degrade with time (Figure 8).

6.1.2. Surface Roughness at Multiple Length Scales

[35] Changes in the pattern of surface roughness also occur as a function of the wavelength over which roughness values are calculated (Figure 9). Each mapped fan unit is characterized by an initial, rapid increase in surface roughness corresponding to an increase in the size of the moving window, over which the standard deviation of slope is determined (Figure 9a). The point at which surface roughness no longer changes rapidly as a function of the size of the averaging window gives an indication of the dominant topographic wavelengths for each surface. As the size of the window becomes larger, surface roughness values for each unit converge when the area over which roughness values are calculated begins to incorporate multiple surfaces (Figure 9a).

[36] Units Q4b, Q4a, Q3c, and Q3b are each characterized by a rapid increase in surface roughness values over wavelengths of five to 12 m, representing the typical length scale of bar and swale topography (Figure 9a). At longer wavelengths, surface roughness values increase by only minor amounts, suggesting the topographic saturation length is ~12 m for the youngest surfaces [e.g., Barabasi and Stanley, 1995]. We note however, the youngest unit, Q4b, appears to have a saturation wavelength that is somewhat longer than units Q4a, Q3c, and Q3b (Figure 9a). This is likely due to the fact that the Q4b channels are often deeply incised through older alluvial fan surfaces (Figure 3a) and therefore, larger averaging windows incorporate steep channel walls, causing higher standard deviations in slope values. A similar pattern emerges for units Q3a and Q2c.

[37] Units Q3a and Q2c show an initial rapid increase in surface roughness values over wavelengths of 5 to 12 m (Figure 9a). However, both the Q3a and Q2c surface roughness values continue to increase steadily at longer wavelengths (Figure 9a). We feel this also occurs as result of active channels (Q4b) being deeply incised through older surfaces (Figure 3a), thus causing standard deviation of slope values to be higher at longer length scales away from the representative central portion of these deposits.

[38] A somewhat different pattern emerges when surface roughness values are analyzed as a function of window size for the two oldest surfaces in the study area, units Q2b and Q2a (Figure 9b). As with the younger units, surface roughness increases at first, although in this case it occurs over a length scale of 50 to 75 m (Figure 9b). The longer topographic saturation wavelength suggests that roughness values on the older surfaces are no longer controlled by the evolution of bar and swale topography. Rather, increased roughness values on these surfaces are the result of headward incision of tributary channels, transforming the once-planar surfaces into rounded hillslopes, leaving behind a signature of topographic roughness at longer wavelengths. Continued incision of tributary streams causes the oldest surface in the study area, Q2a, to have a longer topographic wavelength than the Q2b deposit.

6.1.3. Clast Size Patterns

[39] A pattern similar to that of surface roughness (Figure 8) is observed in the distribution of clast sizes on fan surfaces (Figure 6). A large range of clast sizes is present on the fan surface immediately following deposition. With time, clasts begin to weather and become buried as fan surfaces smooth out [e.g., Bull, 2007]. Absolute clast size and clast-size variance decrease as the fans evolve toward a smooth, stable configuration. As fans continue to increase in age, larger clasts are exhumed from beneath the surface by erosion (Figure 6). Eventually, clast size increases and becomes more variable with age, in much the same way that fan surfaces become rougher.

6.2. Implications for Arid Region Landscape Evolution

[40] Surface roughness, in addition to facilitating the characterization of individual fan units, lends insight to alluvial landform development. We propose an alluvial landform evolutionary scheme that begins with fan deposition within, and downstream from, the mouth of active channels. These areas exhibit prominent bar-and-swale morphology and large variations in clast size. Their surfaces
As turnover occurs over a period of ~70,000 years. As the alluvial fan evolves, stable landform configurations eventually become smooth, planar landforms. In the arid climate of Death Valley, this smoothing process appears to occur over a period of ~70,000 years. As the alluvial fan continues to evolve, stable landform configurations eventually erode into convex hillslopes. Once this threshold is crossed, surface roughness increases with age as tributary

7. Conclusions

[42] Although the surface-roughness data illustrate the progression of fan development with time, at present we are not able to fully quantify the rates over which these processes operate, with the exception of the ~70 ka it apparently takes to evolve from abandonment of the active depositional surface to a stable, planar landform. A recent study by Matmon et al. [2006], in which they investigated the morphologic development of alluvial landforms by measuring cosmogenic nuclide inventories in bars and swales of dated fans, suggests sediment residence times of at least 30,000 years. They suggested that >280,000 years are required for complete smoothing to take place on fans formed along the San Andreas fault in southern California, a significantly longer time interval than we propose for fans in Death Valley. This result emphasizes that rates of alluvial landform evolution are likely to be location-dependent and therefore, calibration for different climatic and tectonic regimes is necessary. Future quantification of the rates of such processes, both through exploitation of high-resolution digital topographic data and by determining the age of individual fan units, will further improve our understanding of postdepositional alluvial landform development.
channel incision dissects the formerly smooth surface. These results demonstrate that diagnostic morphologic features commonly observed on alluvial deposits can be quantified with high-resolution digital topographic data. With access to high-resolution digital topographic data sets becoming more and more common, this methodology will be a useful aid in the objective identification, mapping, and interpretation of alluvial landforms during future studies.

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